

Name:

Enrolment No:



UNIVERSITY OF PETROLEUM AND ENERGY STUDIES
End Semester Examination, December 2019

Course: Advanced Mathematics

Course Code: MATH 7002

Programme: M.Tech (ROE)

Semester: I

Time: 03 hrs.

Max. Marks: 100

Instructions: Attempt all questions from **Section A** (each carrying 4 marks); all questions from **Section B** (each carrying 10 marks) and all questions from **Section C** (carrying 20 marks).

SECTION A

S. No.		Marks	CO
Q1	Determine the value of $\Delta^{10}(1-ax)(1-bx^2)(1-cx^3)(1-dx^4)$.	4	CO1
Q2	Evaluate $\int_0^{1.5} \frac{1}{1+x^3} dx$ using Simpson's 3/8 method, taking $h = 0.25$.	4	CO1
Q3	Determine the value of y at $x = 0.2$ for the differential equation $\frac{dy}{dx} = y + x^2$, $y(0) = 1$ by Euler's method with step size 0.1.	4	CO3
Q4	The regression lines of y on x and x on y are respectively $y = ax + b$, $x = cy + d$. Show that $\frac{\sigma_y}{\sigma_x} = \sqrt{\frac{a}{c}}$.	4	CO5
Q5	Classify the following partial differential equations (i) $2u_{xx} + u_{xy} + 4u_{yy} + u_x = 0$ (ii) $3u_{xx} - 6u_{xy} + 2u_{yy} - 7u_y = 0$.	4	CO4

SECTION B

Q6	Determine a real root of $f(x) = x \sin x + \cos x = 0$ which is near $x = \pi$ correct to three decimal places by using Newton-Raphson's method.	10	CO1
Q7	From the table of half-yearly premium for policies maturing at different ages, estimate the premium for a policy maturing at the age of 63: Age: 45 50 55 60 65 Premium: 114.84 96.16 83.32 74.48 68.48. (in dollars)	10	CO1
Q8	Fit a curve of the form $y = ae^{bx}$ by the method of least square to the data x : 1 5 7 9 12 y : 10 15 12 15 21.	10	CO5
Q9	Solve the differential equation $\frac{dy}{dx} = \log(x+y)$, $y(0) = 2$ by Euler's modified method at $x = 1.2$ and 1.4 with $h = 0.2$.	10	CO3

OR

Q9	Determine the values y of at the pivotal points of the interval $(0,1)$ if y satisfies the boundary value problem $y^{iv} + 81y = 81x^2$, $y(0) = y(1) = y''(0) = y''(1) = 0$. (Take $n=3$)	10	CO3
SECTION-C			
Q10 (A)	Solve the system of equations by Crout's method $3x + 2y + 7z = 4$, $2x + 3y + z = 5$, $3x + 4y + z = 7$.	10	CO2
Q10 (B)	Determine the moment generating function, first four moments about mean and coefficient of skewness and kurtosis for Binomial distribution.	10	CO5
Q11	Solve the equation $u_{xx} + u_{yy} = -10(x^2 + y^2 + 10)$, over the square mesh with sides $x=0, y=0, x=3, y=3$ with $u=0$ on the boundary for fifth iteration only with $h=k=1$ by Liebmann's method.	20	CO4
OR			
Q11 (A)	Solve the equation $u_{tt} = 4u_{xx}$, with $u(0,t) = 0$, $u(4,t) = 0$, $u_t(x,0) = 0$ and $u(x,0) = x(4-x)$ by finite difference method taking $h=1$.	10	CO4
Q11 (B)	Solve the equation $u_t = u_{xx}$, $0 \leq x \leq 1, t \geq 0$, with $u(0,t) = 0$; $u(1,t) = 0$ and $u(x,0) = \begin{cases} 2x & \text{for } 0 \leq x \leq \frac{1}{2} \\ 2(1-x) & \text{for } \frac{1}{2} \leq x \leq 1 \end{cases}$ by using Bender-Schmidt's method.	10	CO4