

Name:

Enrolment No:



## UNIVERSITY OF PETROLEUM AND ENERGY STUDIES

End Semester Examination, May 2021

Programme Name: B Tech EL

Course Name : Electromagnetic Fields & Electrical Materials

Course Code : ECEG2012

Nos. of page(s) : 5

Semester : IV

Time : 03 hrs

Max. Marks : 100

### Instructions:

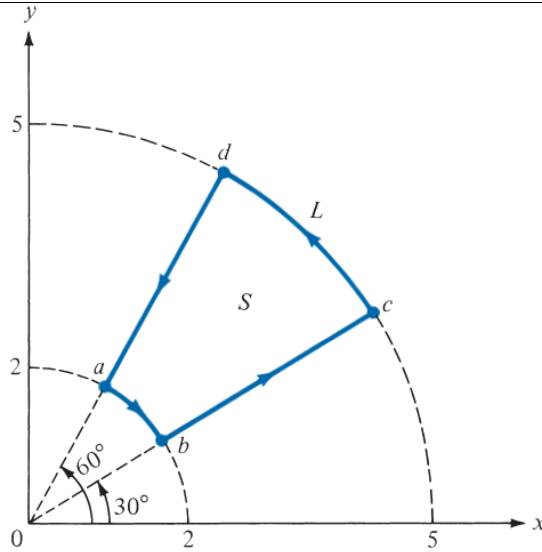
- Attempt all questions.
- Section-A consists 6 questions, first 5 are MCQs.
- Assume any data if required and indicate the same clearly. Unless otherwise indicated symbols and notations have their usual meanings.
- The answer should be neat and clean. Draw a freehand sketch for circuits/tables/schematics wherever required.

### SECTION-A (30 Marks)

|           |  |                |            |
|-----------|--|----------------|------------|
| <b>Q1</b> | <p>(i) Which of these is correct?</p> <p>(a) <math>A \times A =  A ^2</math>                      (b) <math>A \times B + B \times A = 0</math><br/>(c) <math>A \cdot B \cdot C = B \cdot C \cdot A</math>              (d) <math>a_x \cdot a_y = a_z</math><br/>(e) <math>a_k = a_x - a_y</math>, where <math>a_k</math> is a unit vector</p> <p>(ii) Which of the following is zero?</p> <p>(a) grad div                                  (c) curl grad<br/>(b) div grad                                  (d) curl curl</p> <p>(iii) Equation <math>\nabla^2 V = -\rho/\epsilon</math> is called the</p> <p>(a) Poisson's equation                      (b) Laplace equation<br/>(c) Continuity equation                      (d) None</p> <p>(iv) A vector field is given by <math>A = 3xy a_x - y^2 a_y</math>. find <math>\int A \cdot dl</math> along the curve <math>y = 2x^2</math> in the xy plane from (0,0) to (1,2)</p> <p>(a) -9/2      (b) 7/6      (c) -7/6                      (d) 2/3</p> | <b>1+1+1+2</b> | <b>CO1</b> |
| <b>Q2</b> | <p>(i) In a uniform electric field, field lines and equipotential</p> <p>(a) are parallel to one another              (b) intersect at 45°<br/>(c) intersect at 30°                              (d) are orthogonal</p> <p>(ii) When a charge is given to a conductor</p> <p>(a) It distributes uniformly all over the surface<br/>(b) It distributes uniformly all over the volume<br/>(c) It distributes on the surface, inversely proportional to the radius of curvature<br/>(d) It stays where it was placed.</p> <p>(iii) Two infinite parallel metal plates are charged with equal surface charge density of the same polarity. The electric field in the gap b/w the plates is</p>   | <b>1+1+1+2</b> | <b>CO2</b> |

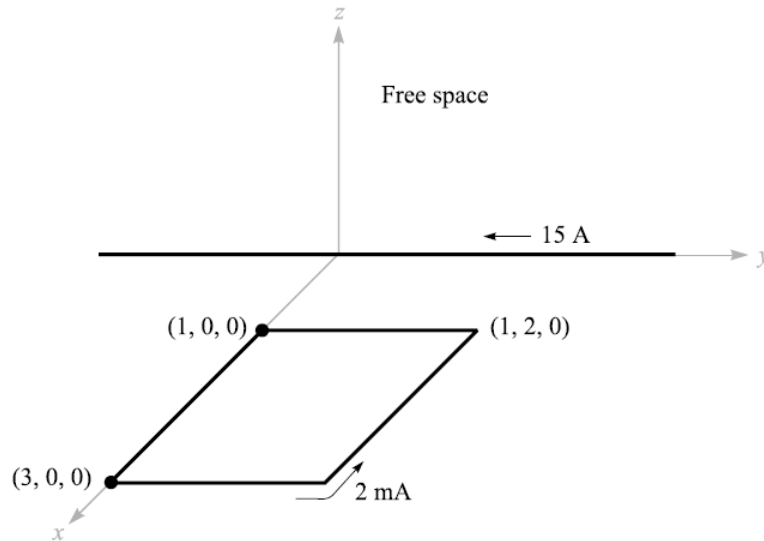


|                             |   |              |            |
|-----------------------------|---|--------------|------------|
|                             | <p>(iii) Given that <math>\mathbf{H} = 0.5 e^{-0.1x} \sin(10^6 t - 2x) \mathbf{a}_z</math> A/m, which of these statements are incorrect?</p> <p>(a) <math>\alpha = 0.1</math> Np/m<br/> <b>(b) <math>\beta = 22</math> rad/m</b><br/> (c) <math>\omega = 10^6</math> rad/s<br/> (d) The wave travels along <math>\mathbf{a}_x</math>.</p>   |              |            |
| <b>Q5</b>                   | <p>(i) Two identical coaxial circular coils carry the same current <math>I</math> but in opposite directions. The magnitude of the magnetic field <math>\mathbf{B}</math> at a point on the axis midway between the coils is</p> <p>(a) Zero<br/> (b) The same as that produced by one coil<br/> (c) Twice that produced by one coil<br/> (d) Half that produced by one coil.</p> <p>(ii) Which of the following statements are not true about electric force <math>\mathbf{F}_e</math> and magnetic force <math>\mathbf{F}_m</math> on a charged particle?</p> <p>(a) <math>\mathbf{E}</math> and <math>\mathbf{F}_e</math> are parallel to each other, whereas <math>\mathbf{B}</math> and <math>\mathbf{F}_m</math> are perpendicular to each other.<br/> (b) Both <math>\mathbf{F}_e</math> and <math>\mathbf{F}_m</math> depend on the velocity of the charged particle.<br/> (c) Both <math>\mathbf{F}_e</math> and <math>\mathbf{F}_m</math> are produced when a charged particle moves at a constant velocity.<br/> (d) <math>\mathbf{F}_m</math> is generally small in magnitude in comparison to <math>\mathbf{F}_e</math>.</p> <p>(iii) Identify the statement that is not true of ferromagnetic materials.</p> <p>(a) They have a large <math>\chi_m</math>.<br/> (b) They have a fixed value of <math>\mu_r</math>.<br/> (c) Energy loss is proportional to the area of the hysteresis loop.<br/> (d) They lose their nonlinearity property above the curie temperature.</p> | <b>2+2+1</b> | <b>CO3</b> |
| <b>Q6</b>                   | State the following laws: Coulomb's law; Gauss law. Also mention the applications of Gauss law.   | <b>5</b>     | <b>CO2</b> |
| <b>SECTION-B (50 Marks)</b> |   |              |            |
| <b>Q1</b>                   | If $A = \rho \cos(\theta) \mathbf{a}_\rho + \sin(\theta) \mathbf{a}_\theta$ , evaluate $\oint A \cdot d\mathbf{l}$ around the path shown in <b>Fig. 1</b> . Confirm this by Stokes's theorem.   | <b>10</b>    | <b>CO1</b> |



**Fig. 1**

|           |  |            |            |
|-----------|--|------------|------------|
|           |  |            |            |
| <b>Q2</b> | <p>(a) A point charge of 5 nC is located at (-3, 4, 0) while the line <math>y = 1, z = 1</math> carries uniform charge of 2 nC/m. If potential <math>V = 0</math> V at O (0, 0, 0), find V at A (5, 0, 1)</p> <p>(b) the finite sheet <math>0 \leq x \leq 1, 0 \leq y \leq 1</math> on the <math>z = 0</math> plane has a charge density <math>\rho_s = xy(x^2 + y^2 + 25)^{3/2}</math> nC/m<sup>2</sup>. Find the total charge on the sheet and electric field at (0, 0, 5).</p>  | <b>5+5</b> | <b>CO2</b> |
| <b>Q3</b> | <p>Two extensive homogeneous isotropic dielectric meets on plane <math>z = 0</math>. For <math>z &gt; 0, \epsilon_{r1} = 4</math> and for <math>z &lt; 0, \epsilon_{r2} = 3</math>. A uniform electric field <math>E_1 = 5a_x - 2a_y + 3a_z</math> kV/m exists for <math>z \geq 0</math>. Find</p> <p>(a) <math>E_2</math> for <math>z \leq 0</math>;</p> <p>(b) the angles <math>E_1</math> and <math>E_2</math> make with the interface;</p> <p>(c) the energy densities (in J/m<sup>3</sup>) in both dielectrics;</p> | <b>10</b>  | <b>CO2</b> |
| <b>Q4</b> | <p>Find the magnetic field intensity H at (-3, 4, 0) due to current filament shown in <b>Fig. 2</b></p>  | <b>10</b>  | <b>CO3</b> |
|           | <p><b>Fig. 2</b></p>   |            |            |
| <b>Q5</b> | <p>(a) A square loop of wire in the <math>z = 0</math> plane carrying 2 mA in the field of an infinite filament on the y axis, as shown in <b>Fig.3</b> find the total force on the loop.</p>  | <b>5+5</b> | <b>CO3</b> |



**Fig.3**

(b) Let us assume that  $\mu = \mu_1 = 4 \mu\text{H/m}$  in region 1 where  $z > 0$ , whereas  $\mu_2 = 7 \mu\text{H/m}$  in region 2 wherever  $z < 0$ . Moreover, let  $\mathbf{K} = 80 \mathbf{a}_x \text{ A/m}$  on the surface  $z = 0$ . We establish a field,  $\mathbf{B}_1 = 2\mathbf{a}_x - 3\mathbf{a}_y + \mathbf{a}_z \text{ mT}$ , in region 1 and find the value of  $\mathbf{B}_2$ .

**SECTION-C (20 Marks)**

- Q1** A plane wave with  $E = 30e^{-\alpha z} \sin(\omega t - z) \mathbf{a}_x \text{ V/m}$  is propagating through a lossy dielectric medium having an intrinsic impedance of  $300 \angle 30^\circ$  and  $\mu_r = 1$ .
- Determine the phasor and instantaneous field expressions for H
  - Find the loss tangent, propagation constant, wave polarization and the dielectric constant of the medium at 15 MHz
  - Determine the skin depth and the depth at which the amplitude of the field is 1% of the value at  $z=0$ .

**OR**

A plane wave travelling in the  $+z$  direction in free space ( $z < 0$ ) is normally incident at  $z = 0$  on a conductor ( $z > 0$ ) for which  $\sigma = 61.7 \text{ MS/m}$ ,  $\mu_r = 1$ . The free space wave has a frequency of 2.5 MHz. the E field amplitude is 1.5 V/m at the interface. Find the expression for H in the conductor. Also find the loss tangent and skin depth.

**20**

**CO4**